

IX Računske vežbe

① Predajna prostorija je industrijska hala, a prijemna konstrukcijski biro koji se nalazi iznad hale. Nivo buke v proizvodnoj hali je 90 dB. Da li je nivo buke v konstrukcijskom birovu, dimenzija 10x6x5m, sa srednjom vrednošću koeficijenta apsorpcije 0,4 v dozvoljenim granicama, ako je srednja vrednost koeficijenta prenošenja tavanice 0,01? Dozvoljeni nivo buke v konstrukcijskom birovu iznosi 45 dB. (14. knjiga)

$$L_1 = 90 \text{ dB}$$

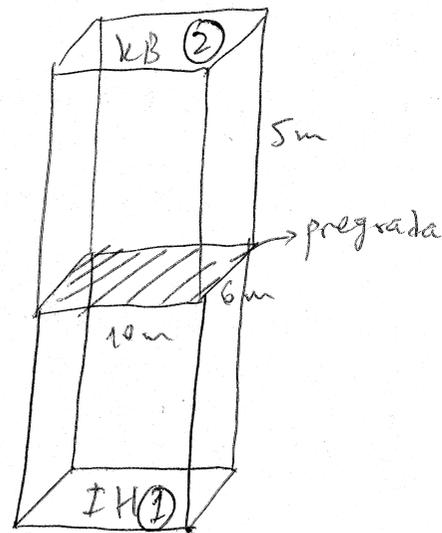
$$KB: 10 \times 6 \times 5 \text{ m}$$

$$\left. \begin{array}{l} a_2 = 10 \text{ m} \\ b_2 = 6 \text{ m} \\ c_2 = 5 \text{ m} \end{array} \right\} V_2 = a_2 b_2 c_2 = 10 \cdot 6 \cdot 5 \text{ m}^3 = \boxed{300 \text{ m}^3}$$

$$\bar{\alpha}_2 = 0,4$$

$$\bar{\tau} = 0,01 \text{ (1\%)}$$

$$L_{2d} = 45 \text{ dB}$$



$$S_2 = 2(a_2 b_2 + a_2 c_2 + b_2 c_2)$$

$$S_2 = 2 \cdot (10 \cdot 6 + 10 \cdot 5 + 6 \cdot 5) = 2 \cdot (60 + 50 + 30) = 2 \cdot 140 = \boxed{280 \text{ m}^2}$$

$$\boxed{S_2 = 280 \text{ m}^2} - \text{površina konstrukcijskog biroa}$$

$$A_2 = \sum_i S_i \alpha_i = S_2 \bar{\alpha}_2 = 280 \cdot 0,4 = \boxed{112 \text{ m}^2}$$

$$R = 10 \log \left(\frac{P_1}{P_2} \right) = 10 \log \left(\frac{\frac{I_1 S_P}{r}}{\frac{I_2 A_2}{r}} \right) = 10 \log \left(\frac{I_1}{I_2} \cdot \frac{S_P}{A_2} \right) = \underbrace{10 \log \frac{I_1}{I_2}}_{D = L_1 - L_2} + 10 \log \frac{S_P}{A_2}$$

$$\Rightarrow \boxed{R = D + 10 \log \frac{S_P}{A_2}}$$

S_P - površina pregrade

$$D = L_1 - L_2 = R - 10 \log \frac{S_p}{A_2} = \boxed{R + 10 \log \frac{A_2}{S_p}}$$

$$\boxed{R = 10 \log \left(\frac{1}{\epsilon} \right)}$$

$$R = 10 \log \left(\frac{1}{10^{-2}} \right) = 10 \log (10^2) = 2 \cdot 10 \cdot \log 10^1 = \boxed{20 \text{ dB}} \quad \boxed{R = 20 \text{ dB}}$$

$$D = R + 10 \log \frac{A_2}{S_p}$$

$$S_p = 10 \cdot 6 = \boxed{60 \text{ m}^2}$$

$$D = R + 10 \log \left(\frac{112 \text{ m}^2}{60 \text{ m}^2} \right) = R + 10 \log \left(\frac{56}{30} \right) = R + \underbrace{10 \log \left(\frac{28}{15} \right)}_{2,7 \text{ dB}}$$

$$\boxed{D = 22,7 \text{ dB}}$$

$$D = L_1 - L_2 = R + 10 \log \frac{A_2}{S_p}$$

$$L_2 = L_1 - R - 10 \log \frac{A_2}{S_p}$$

$$L_2 = 90 - 20 - 10 \log \left(\frac{112}{60} \right) = 70 - \underbrace{10 \log \left(\frac{28}{15} \right)}_{2,7} = \boxed{67,3 \text{ dB}}$$

$$\boxed{L_2 = 67,3 \text{ dB}}$$

$$DL = L_1 - L_2 = 90 \text{ dB} - 67,3 \text{ dB} = \boxed{22,7 \text{ dB}}$$

$DL = 22,3 \text{ dB}$ - preukračenje v kB

2) Dve susedne prostorije oblika kocke, stranice 4m, imaju istu srednju vrednost koeficijenta apsorpcije 0,3. V predajnoj prostoriji smešten je izvor zvuka zvučne snage 10 W. Odrediti:

- (a) intenzitet difuznog zvuka v predajnoj prostoriji
 (b) intenzitet v prijemnoj prostoriji pri koeficijentu prenosjenja pregradnog zida 0,01
 (c) intenzitet zvuka v prostoriji ako se ukloni pregradni zid. (15. enjiga)

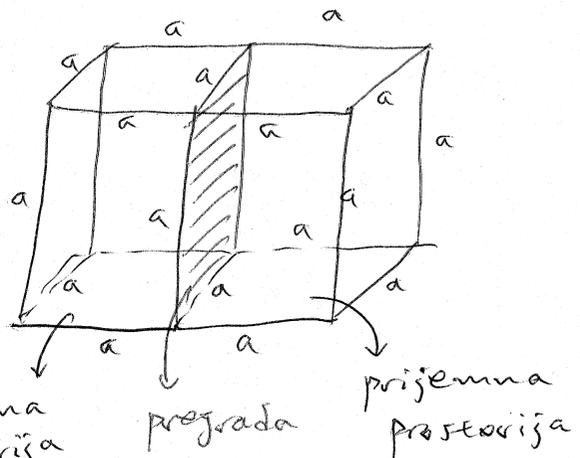
$$a = 4 \text{ m}$$

$$\bar{\alpha}_1 = \bar{\alpha}_2 = \bar{\alpha} = 0,3$$

$$P_a = 10 \text{ W} = 10 \cdot 10^{-3} \text{ W} = 10^{-2} \text{ W}$$

$$S_1 = S_2 = 6a^2 = 6 \cdot 4^2 = 6 \cdot 16 = 96 \text{ m}^2$$

$$A = \sum_i S_i \bar{\alpha}_i = S_1 \bar{\alpha}_1 = 96 \cdot 0,3 = 28,8 \text{ m}^2 \text{ predajna prostorija}$$



(a)
$$I_1 = \frac{4 P_a}{A_1} = \frac{4 \cdot 10^{-2}}{28,8} \frac{\text{W}}{\text{m}^2} = 1,39 \cdot 10^{-3} \frac{\text{W}}{\text{m}^2}$$

$$L_1 = 10 \log \frac{I_1}{I_0} = 10 \log \left(\frac{1,39 \cdot 10^{-3} \frac{\text{W}}{\text{m}^2}}{10^{-12} \frac{\text{W}}{\text{m}^2}} \right) = 10 \log (1,39 \cdot 10^9) = 10 \log (1,39) + 10 \log 10^9 = 10 \log (1,39) + 90 = 91,4 \text{ dB}$$

$$L_1 = 91,4 \text{ dB}$$

(b) pregradni zid: $S_p = S_{12} = a \cdot a = a^2 = 16 \text{ m}^2$

$$\bar{\tau} = 0,01 \text{ (1\%)}$$

$$R = 10 \log \left(\frac{1}{\bar{\tau}} \right) = 10 \log \left(\frac{1}{10^{-2}} \right) = 10 \log (10^2) = 10 \cdot 2 \cdot \log 10 = 20 \text{ dB}$$

$$R = 20 \text{ dB}$$

$$A_2 = A_1 = 28,8 \text{ m}^2$$

$$D = R + 10 \log \frac{A_2}{S_p} = 20 + 10 \log \left(\frac{28,8 \text{ m}^2}{16 \text{ m}^2} \right) = 20 + 10 \log \left(\frac{28,8}{16} \right) =$$

$$= 20 + 10 \log(1,8) = \boxed{22,5 \text{ dB}} \Rightarrow \boxed{D = 22,5 \text{ dB}}$$

$$D = L_1 - L_2 \Rightarrow L_2 = L_1 - D = (91,4 - 22,5) \text{ dB} = \boxed{68,9 \text{ dB}}$$

$$\boxed{D = 68,9 \text{ dB}}$$

$$L_2 = 10 \log \frac{I_2}{I_0} \Rightarrow \frac{L_2}{10} = \log \frac{I_2}{I_0} \Rightarrow 10^{\frac{L_2}{10}} = \frac{I_2}{I_0} \Rightarrow \boxed{I_2 = I_0 \cdot 10^{\frac{L_2}{10}}}$$

$$I_0 = 10^{-12} \frac{\text{W}}{\text{m}^2}$$

$$I_2 = 10^{-12} \cdot 10^{\frac{68,9}{10}} \frac{\text{W}}{\text{m}^2} = 10^{-12} \cdot 10^{6,89} \frac{\text{W}}{\text{m}^2} = 10^{-12+6,89} \frac{\text{W}}{\text{m}^2} = 10^{-5,11} \frac{\text{W}}{\text{m}^2}$$

$$\Rightarrow \boxed{I_2 = 7,76 \cdot 10^{-6} \frac{\text{W}}{\text{m}^2}}$$

$$\textcircled{c} S = 2 \cdot (2a \cdot a + 2a \cdot a + a \cdot a) = 2 \cdot (2a^2 + 2a^2 + a^2) = 2 \cdot 5a^2 = 10a^2$$

$$S = 12a^2 - 2a^2 = 10a^2 \Rightarrow S = 10 \cdot 4^2 = 10 \cdot 16 = \boxed{160 \text{ m}^2}$$

$\boxed{S = 160 \text{ m}^2}$ - površina kada se vulfoni progradni zid između predajne i prijemne prostorije

$$A = \sum_i S_i d_i = S \bar{d} = 160 \cdot 0,3 \text{ m} = \boxed{48 \text{ m}^2}$$

$$I = \frac{4 \text{ Pa}}{A} = \frac{4 \cdot 10^{-2} \text{ W}}{48 \text{ m}^2} = \frac{1}{12} \cdot 10^{-2} \frac{\text{W}}{\text{m}^2} = \boxed{8,3 \cdot 10^{-4} \frac{\text{W}}{\text{m}^2}}$$

$$L = 10 \log \frac{I}{I_0} = 10 \log \left(\frac{8,3 \cdot 10^{-4} \frac{\text{W}}{\text{m}^2}}{10^{-12} \frac{\text{W}}{\text{m}^2}} \right) = 10 \log (8,3 \cdot 10^8) =$$

$$= 10 \log(8,3) + 10 \log(10^8) = 10 \log(8,3) + 10 \cdot 8 \cdot \log 10 =$$

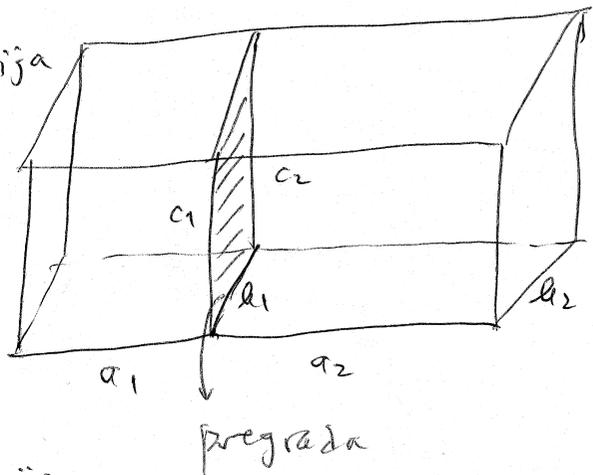
$$= 80 + 10 \log(8,3) = \boxed{89,2 \text{ dB}}$$

$$\Rightarrow \boxed{L = 89,2 \text{ dB}}$$

3. Odrediti zvučnu snagu izvora i intenzitet zvuka u prostoriji dimenzija $10 \times 8 \times 5 \text{ m}$ i srednje vrednosti koeficijenta refleksije zvuka $0,7999$, koja je od prijemne prostorije odvojena pregradnim zidom ukupne zvučne izolacije $47,78 \text{ dB}$. U prijemnoj prostoriji dimenzija $20 \times 8 \times 5 \text{ m}$ i srednje vrednosti koeficijenta apsorpcije zvuka $0,4$, izmeren je intenzitet zvuka $0,4 \frac{\text{mW}}{\text{m}^2}$. (16. knjiga)

$$\begin{aligned} a_1 &= 10 \text{ m} \\ b_1 &= 8 \text{ m} \\ c_1 &= 5 \text{ m} \\ \bar{r}_1 &= 0,7999 \end{aligned}$$

predajna prostorija



$$D = 47,78 \text{ dB}$$

$$\begin{aligned} a_2 &= 20 \text{ m} \\ b_2 &= 8 \text{ m} \\ c_2 &= 5 \text{ m} \\ \bar{d}_2 &= 0,4 \\ \bar{r}_2 &= 0,4 \frac{\text{mW}}{\text{m}^2} \end{aligned}$$

prijemna prostorija

$$S_1 = 2(a_1 b_1 + a_1 c_1 + b_1 c_1) = 2 \cdot (10 \cdot 8 + 10 \cdot 5 + 8 \cdot 5) = 2 \cdot (80 + 50 + 40)$$

$$S_1 = 2 \cdot 170 = \boxed{340 \text{ m}^2} \Rightarrow \boxed{S_1 = 340 \text{ m}^2}$$

$$S_2 = 2(a_2 b_2 + a_2 c_2 + b_2 c_2) = 2 \cdot (20 \cdot 8 + 20 \cdot 5 + 8 \cdot 5) = 2 \cdot (160 + 100 + 40)$$

$$S_2 = 2 \cdot 300 = \boxed{600 \text{ m}^2} \Rightarrow \boxed{S_2 = 600 \text{ m}^2}$$

$$A_2 = \sum_i S_i \bar{d}_i = S_2 \bar{d}_2 = 600 \cdot 0,4 \text{ m}^2 = \boxed{240 \text{ m}^2}$$

$$S_p = S_{12} = 8 \cdot 5 = \boxed{40 \text{ m}^2}$$

$$D = R + 10 \log \frac{A_2}{S_p}$$

$$R = D - 10 \log \frac{A_2}{S_p} = 47,78 - 10 \log \left(\frac{24 \text{ dB}}{4 \text{ dB}} \right) = 47,78 - \frac{10 \log 6}{7,78} = \boxed{40 \text{ dB}}$$

$$\Rightarrow \boxed{R = 40 \text{ dB}}$$

$$R = 10 \log \left(\frac{1}{\bar{\tau}} \right) \Rightarrow \frac{R}{10} = \log \left(\frac{1}{\bar{\tau}} \right)$$

$$10 \frac{R}{10} = \frac{1}{\bar{\tau}} \Rightarrow \bar{\tau} = \frac{1}{10 \frac{R}{10}} \Rightarrow \boxed{\bar{\tau} = 10^{-\frac{R}{10}}}$$

$$\bar{\tau} = 10^{-\frac{40}{10}} = 10^{-4} = 0,0001$$

$$I_2 = \frac{4 P_2}{A_2} \Rightarrow \boxed{P_2 = \frac{A_2 I_2}{4}}$$

$$P_2 = \frac{24 \text{ dB} \cdot 0,4 \cdot 10^{-3} \frac{\text{W}}{\text{m}^2}}{4} = 60 \cdot 0,4 \cdot 10^{-3} \text{ W} = \boxed{24 \cdot 10^{-3} \text{ W}}$$

$$\boxed{P_2 = 0,024 \text{ W}}$$

$$\boxed{P_2 = 24 \text{ mW}}$$

$$\bar{\tau} = \frac{P_2}{P_1} \Rightarrow P_1 = \frac{P_2}{\bar{\tau}} = \frac{24 \cdot 10^{-3} \text{ W}}{10^{-4}} = 24 \cdot 10 \text{ W} \Rightarrow \boxed{P_1 = 240 \text{ W}}$$

$$P_1 = \frac{I_1 S_p}{4} \Rightarrow I_1 = \frac{4 P_1}{S_p} = \frac{4 \cdot 240 \text{ W}}{40 \text{ m}^2} = \boxed{24 \frac{\text{W}}{\text{m}^2}}$$

$$\bar{\alpha}_1 + \bar{r}_1 + \bar{\tau} = 1$$

$$\bar{\alpha}_1 = 1 - \bar{r}_1 - \bar{\tau} = 1 - 0,0001 - 0,7999 = 1 - 0,8 = \boxed{0,2} \Rightarrow \boxed{\bar{\alpha}_1 = 0,2}$$

$$\boxed{S_1 = 340 \text{ m}^2}$$

$$A_1 = \sum_i S_i \bar{\alpha}_i = S_1 \bar{\alpha}_1 = 340 \cdot 0,2 \text{ m}^2 = \boxed{68 \text{ m}^2}$$

$$I_1 = \frac{4 P_a}{A_1} \Rightarrow P_a = \frac{I_1 A_1}{4} = \frac{24 \frac{\text{W}}{\text{m}^2} \cdot 68 \text{ m}^2}{4} = \frac{24 \cdot 68 \text{ W}}{4} = 6 \cdot 68 \text{ W}$$

$$\Rightarrow \boxed{P_a = 408 \text{ W}}$$

4. Izvor zvuka se nalazi u proizvodnoj hali dimenzija $10 \times 8 \times 4$ m i srednje vrednosti koeficijenta refleksije 0,6. Hala je od kancelarijskog prostora, dimenzija $8 \times 4 \times 4$ m i srednje vrednosti koeficijenta apsorpcije 0,5, odvojena pregradnim zidom koji obezbeđuje ukupnu zvučnu izolaciju prostora od 40 dB. Izračunati zvučnu snagu izvora zvuka ako je nivo zvuka u kancelarijskom prostoru 70 dB. (17. maja)

$$\left. \begin{array}{l} a_1 = 10 \text{ m} \\ b_1 = 8 \text{ m} \\ c_1 = 4 \text{ m} \\ \bar{\alpha}_1 = 0,6 \end{array} \right\} \begin{array}{l} \text{proizvodna} \\ \text{hala} \end{array} \quad \left. \begin{array}{l} a_2 = 8 \text{ m} \\ b_2 = 4 \text{ m} \\ c_2 = 4 \text{ m} \\ \bar{\alpha}_2 = 0,5 \end{array} \right\} \text{kancelarija}$$

$$D = 40 \text{ dB}$$

$$L_2 = 70 \text{ dB}$$

$$P_a = ?$$

$$D = L_1 - L_2 \Rightarrow L_1 = L_2 + D = 70 \text{ dB} + 40 \text{ dB} = \boxed{110 \text{ dB}}$$

$$\boxed{L_1 = 110 \text{ dB}} \quad L_1 = 10 \log \frac{I_1}{I_0} \Rightarrow \frac{L_1}{10} = \log \frac{I_1}{I_0} \Rightarrow 10^{\frac{L_1}{10}} = \frac{I_1}{I_0} \Rightarrow \boxed{I_1 = I_0 \cdot 10^{\frac{L_1}{10}}}$$

$$I_0 = 10^{-12} \frac{\text{W}}{\text{m}^2}$$

$$I_1 = 10^{-12} \frac{\text{W}}{\text{m}^2} \cdot 10^{\frac{110}{10}} = 10^{-12} \cdot 10^{11} \frac{\text{W}}{\text{m}^2} = 10^{-1} \frac{\text{W}}{\text{m}^2} = \boxed{0,1 \frac{\text{W}}{\text{m}^2}}$$

$$\boxed{I_1 = 0,1 \frac{\text{W}}{\text{m}^2}}$$

$$S_1 = 2(a_1 b_1 + a_1 c_1 + b_1 c_1) = 2 \cdot (10 \cdot 8 + 10 \cdot 4 + 8 \cdot 4) = 2 \cdot (80 + 40 + 32)$$

$$S_1 = 2 \cdot 152 = \boxed{304 \text{ m}^2} \Rightarrow \boxed{S_1 = 304 \text{ m}^2}$$

$$S_2 = 2(a_2 b_2 + a_2 c_2 + b_2 c_2) = 2 \cdot (8 \cdot 4 + 8 \cdot 4 + 4 \cdot 4) = 2 \cdot (32 + 32 + 16) =$$

$$= 2 \cdot 80 = 160 = \boxed{160 \text{ m}^2} \Rightarrow \boxed{S_2 = 160 \text{ m}^2}$$

$$A_2 = \sum_i S_i d_i = S_2 \bar{d}_2 = 160 \cdot 0,5 = \boxed{80 \text{ m}^2}$$

$$S_p = S_{12} = 8 \cdot 4 = \boxed{32 \text{ m}^2}$$

$$R = D - 10 \log \frac{A_2}{S_{12}} = 40 - 10 \log \left(\frac{80}{32} \right) = 40 - \underbrace{10 \log \left(\frac{5}{2} \right)}_4 = \boxed{36 \text{ dB}}$$

$$\boxed{R = 36 \text{ dB}}$$

$$R = 10 \log \left(\frac{1}{\bar{\epsilon}} \right) \Rightarrow \frac{R}{10} = \log \left(\frac{1}{\bar{\epsilon}} \right) \Rightarrow 10^{\frac{R}{10}} = \frac{1}{\bar{\epsilon}} \Rightarrow \boxed{\bar{\epsilon} = 10^{-\frac{R}{10}}}$$

$$\bar{\epsilon} = 10^{-\frac{36}{10}} = 10^{-3,6} \Rightarrow \boxed{\bar{\epsilon} = 2,5 \cdot 10^{-4}}$$

$$\bar{d}_1 + \bar{r}_1 + \bar{\epsilon} = 1$$

$$\bar{d}_1 = 1 - \bar{r}_1 - \bar{\epsilon} = 1 - 0,00025 - 0,6 = 0,4 - 0,00025 = \boxed{0,39975}$$

$$\Rightarrow \boxed{\bar{d}_1 = 0,39975}$$

$$\boxed{S_1 = 304 \text{ m}^2}$$

$$A_1 = \sum_i S_i d_i = S_1 \bar{d}_1 = 304 \cdot 0,39975 = \boxed{121,5 \text{ m}^2}$$

$$I_1 = \frac{4 P_a}{A_1} \Rightarrow P_a = \frac{I_1 A_1}{4} = \frac{0,1 \frac{\text{W}}{\text{m}^2} \cdot 121,5 \text{ m}^2}{4} = \frac{0,1 \cdot 121,5 \text{ W}}{4}$$

$$P_a = \frac{12,15 \text{ W}}{4} \Rightarrow \boxed{P_a = 3,04 \text{ W}}$$

5. Pregrada ukupne površine 28 m^2 sačinjena od zida izolacione moći 48 dB i vrata površine 2 m^2 , čija je izolaciona moć 25 dB . Ako se na pregradu postavi i prozor površine 8 m^2 , izračunati potrebnu izolacionu moć prozora kako se izolaciona moć pregrade ne bi pogoršala za više od 1 dB . (18. rujna)

$$S_{12} = 28 \text{ m}^2 - \text{površina pregrade}$$

$$R_z = 48 \text{ dB} - \text{izolaciona moć zida}$$

$$S_v = 2 \text{ m}^2 - \text{površina vrata}$$

$$R_v = 25 \text{ dB} - \text{izolaciona moć vrata}$$

$$S_p = 8 \text{ m}^2 - \text{površina prozora}$$

$$R_p = ? - \text{izolaciona moć prozora}$$

$$S_{12} = S_z + S_v \quad (\text{zid} + \text{vrata})$$

$$S_z = S_{12} - S_v = 28 - 2 = \boxed{26 \text{ m}^2} - \text{površina zida}$$

$$S_{12} \cdot \bar{\tau}_{12} = S_z \cdot \bar{\tau}_z + S_v \cdot \bar{\tau}_v \quad (*)$$

$$R_z = 10 \log\left(\frac{1}{\bar{\tau}_z}\right) \Rightarrow \frac{R_z}{10} = \log\left(\frac{1}{\bar{\tau}_z}\right) \Rightarrow 10^{\frac{R_z}{10}} = \frac{1}{\bar{\tau}_z}$$

$$\boxed{\bar{\tau}_z = 10^{-\frac{R_z}{10}}}$$

$$R_v = 10 \log\left(\frac{1}{\bar{\tau}_v}\right) \Rightarrow \frac{R_v}{10} = \log\left(\frac{1}{\bar{\tau}_v}\right) \Rightarrow 10^{\frac{R_v}{10}} = \frac{1}{\bar{\tau}_v}$$

$$\boxed{\bar{\tau}_v = 10^{-\frac{R_v}{10}}}$$

$$R_p = 10 \log\left(\frac{1}{\bar{\tau}_p}\right) \Rightarrow \frac{R_p}{10} = \log\left(\frac{1}{\bar{\tau}_p}\right) \Rightarrow 10^{\frac{R_p}{10}} = \frac{1}{\bar{\tau}_p}$$

$$\boxed{\bar{\tau}_p = 10^{-\frac{R_p}{10}}}$$

$$(*) \Rightarrow \bar{T}_n = \frac{S_z \bar{T}_z + S_v \bar{T}_v}{S_{12}} = \frac{S_z \cdot 10^{-\frac{R_z}{10}} + S_v \cdot 10^{-\frac{R_v}{10}}}{S_{12}}$$

$$R_n = 10 \log \left(\frac{1}{\bar{T}_n} \right) = 10 \log \left(\frac{1}{\frac{S_z \cdot 10^{-\frac{R_z}{10}} + S_v \cdot 10^{-\frac{R_v}{10}}}{S_{12}}} \right)$$

$$R_n = 10 \log \left(\frac{S_{12}}{S_z \cdot 10^{-\frac{R_z}{10}} + S_v \cdot 10^{-\frac{R_v}{10}}} \right)$$

$$R_n = 10 \log \left(\frac{28}{26 \cdot 10^{-\frac{48}{10}} + 2 \cdot 10^{-\frac{25}{10}}} \right) = 10 \log \left(\frac{14}{13 \cdot 10^{-4,8} + 10^{-2,5}} \right)$$

$$R_n = 36,2 \text{ dB}$$

$$R_n' = R_n - 1 \Rightarrow R_n' = 35,2 \text{ dB}$$

S_z' - površina zida nakon postavljanja prozora

$$S_z' = S_{12} - S_v - S_p = 28 - 2 - 8 = 18 \text{ m}^2$$

$$\bar{T}_n' = \frac{S_z' \bar{T}_z + S_v \bar{T}_v + S_p \bar{T}_p}{S_{12}} = \frac{S_z' \cdot 10^{-\frac{R_z}{10}} + S_v \cdot 10^{-\frac{R_v}{10}} + S_p \cdot 10^{-\frac{R_p}{10}}}{S_{12}}$$

$$R_n' = 10 \log \left(\frac{1}{\bar{T}_n'} \right) = 10 \log \left(\frac{1}{\frac{S_z' \cdot 10^{-\frac{R_z}{10}} + S_v \cdot 10^{-\frac{R_v}{10}} + S_p \cdot 10^{-\frac{R_p}{10}}}{S_{12}}} \right)$$

$$\frac{R_n'}{10} = \log \frac{S_{12}}{S_z' \cdot 10^{-\frac{R_z}{10}} + S_v \cdot 10^{-\frac{R_v}{10}} + S_p \cdot 10^{-\frac{R_p}{10}}}$$

$$10^{\frac{R_n'}{10}} = \frac{S_{12}}{S_z' \cdot 10^{-\frac{R_z}{10}} + S_v \cdot 10^{-\frac{R_v}{10}} + S_p \cdot 10^{-\frac{R_p}{10}}}$$

$$S_z' \cdot 10^{-\frac{R_z}{10}} + S_v \cdot 10^{-\frac{R_v}{10}} + S_p \cdot 10^{-\frac{R_p}{10}} = S_{12} \cdot 10^{-\frac{R_n'}{10}} \quad | : S_p$$

$$S_p \cdot 10^{-\frac{P_p}{10}} = S_{12} \cdot 10^{-\frac{P_{n1}}{10}} - S_2^1 \cdot 10^{-\frac{P_2}{10}} - S_v \cdot 10^{-\frac{P_v}{10}} \quad | : S_p$$

$$10^{-\frac{P_p}{10}} = \frac{1}{S_p} \left[S_{12} \cdot 10^{-\frac{P_{n1}}{10}} - S_2^1 \cdot 10^{-\frac{P_2}{10}} - S_v \cdot 10^{-\frac{P_v}{10}} \right] \quad | \log_{10}$$

$$-\frac{P_p}{10} = \log_{10} \left[\frac{1}{S_p} \left(S_{12} \cdot 10^{-\frac{P_{n1}}{10}} - S_2^1 \cdot 10^{-\frac{P_2}{10}} - S_v \cdot 10^{-\frac{P_v}{10}} \right) \right] \quad | \cdot (-10)$$

$$P_p = 10 \log \left[\frac{S_p}{S_{12} \cdot 10^{-\frac{P_{n1}}{10}} - S_2^1 \cdot 10^{-\frac{P_2}{10}} - S_v \cdot 10^{-\frac{P_v}{10}}} \right]$$

$$P_p = 10 \log \left(\frac{8}{28 \cdot 10^{-\frac{35,2}{10}} - 18 \cdot 10^{-\frac{4,8}{10}} - 2 \cdot 10^{-\frac{2,5}{10}}} \right)$$

$$P_p = 10 \log \left(\frac{4}{14 \cdot 10^{-3,52} - 9 \cdot 10^{-4,8} - 10^{-2,5}} \right) = \boxed{36,4 \text{ dB}}$$

$P_p = 36,4 \text{ dB}$ izolacyjna moc
przebiega